

# CRUX MATHEMATICORUM

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## SYNOPSIS

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**1 Letter from the Editor / Lettre des rédacteurs.**

Some information on the change of editorship, change in subscription rates, and change in schedule for *CRUX*.

**3 CONGRATULATIONS** to Professor Ron Dunkley, Canadian Mathematics Competitions, on being elected as a Member of the Order of Canada.

**3 Guidelines for Articles.** by Denis Hanson.

**4 Unitary Divisor Problems:** K.R.S. Sastry.

Sastry introduces the unitary extension of super-abundant numbers, and proves some results:

**Theorem 1:** Let  $n = \prod_{i=1}^k p_i^{\alpha_i}$  denote the prime decomposition of  $n$  and  $D^* = \{d^* : d^* \text{ is a unitary divisor of } n\}$ . Then

$$\sum \phi(d^*) = \prod_{i=1}^k [1 + \phi(p_i^{\alpha_i})].$$

**Theorem 2:** Let  $p_k$  denote the  $k^{\text{th}}$  prime,  $k = 1, 2, \dots$ . Then  $n = p_1 p_2 \cdots p_k$  is a unitary super abundant number.

**Theorem 3:** The only unitary super abundant numbers are

$$n_k, \quad k = 1, 2, 3, \dots$$

That is

$$2, 6, 30, 210, 2310, \dots$$

- 10 **The Skoliad Corner:** No. 11 R.E. Woodrow.  
Featuring the **SHARP U.K. INTERMEDIATE MATH CHALLENGE** and the “official” solutions to the Saskatchewan Senior Mathematics Contest 1994.
- 20 **A Historical Titbit**, featuring a problem taken from a 1894 Ontario Public School textbook.
- 21 **The Olympiad Corner:** No. 171 R.E. Woodrow.  
Featuring the 29th Spanish Mathematical Olympiad National Round, six Klamkin Quickies, and solutions to problems from the 43rd Mathematical Olympiad (1991–1992) in Poland.
- 27 A short **Biography** of the new Editor-in-Chief.
- 28 **The Academy Corner:** No. 1 Bruce Shawyer.  
Introducing a new Corner featuring University Undergraduate Mathematics Competitions, starting with the 1995 Memorial University Undergraduate Mathematics Competition.
- 29 **Mathematical Literacy:** some interesting questions about the history of mathematics.
- 30 **Book Reviews:** Andy Liu.  
*The Monkey and the Calculator (Le singe et la calculatrice)*,  
*Aladdin's Sword (Le sabre d'Aladin)*.  
Both published in 1995 by Production et Organisation du Loisir Educatif (POLE) 31 avenue des Gobelins, 75013 Paris, France.  
Both reviewed by *Claude Laflamme*, University of Calgary.  
*Tournament of the Towns, 1980-1984, Questions and Solutions*,  
*Tournament of the Towns, 1989-1993, Questions and Solutions*.  
Both edited by Peter J. Taylor, Australian Mathematics Trust, University of Canberra, P.O. Box 1, Belconnen, A.C.T. 2616, Australia.  
Both reviewed by *Murray S. Klamkin*, University of Alberta.
- 33 **Problems:** 2101-2113.  
This month's “free sample” is:  
**2102.** *Proposed by Toshio Seimiya, Kawasaki, Japan.*  
*ABC* is a triangle with incentre *I*. Let *P* and *Q* be the feet of the perpendiculars from *A* to *BI* and *CI* respectively. Prove that
- $$\frac{AP}{BI} + \frac{AQ}{CI} = \cot \frac{A}{2}.$$
- 36 **Solutions:** 1827, 2006-2010, 2012-2015.