Linear Combinations of Composition Operators on the Bloch Spaces

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Abstract. We characterize the compactness of linear combinations of analytic composition operators on the Bloch space. We also study their boundedness and compactness on the little Bloch space.

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