Curve counting on (K3xE)/G and Siegel modular forms

For a cyclic group G of order N acting symplectically on a K3 surface S and by translation on an elliptic curve E, we consider the Calabi-Yau threefold X given by $X = (S \times E)/G$. We conjecture that the Donaldson-Thomas partition function of Xis given by a certain genus 2 Siegel modular form Φ_N which is of weight $\lceil \frac{24}{N+1} \rceil - 2$. We provide strong evidence for the conjecture and discuss the connection with CHL models in physics, Mathieu moonshine, and elliptic genera.

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