I will discuss some of my recent work on problems connected to the construction of measures with fractal support and whose Fourier transform decays rapidly at infinity.