An infinite family of self-dual embeddings of strongly regular self-complementary graphs is presented. These embeddings are very highly structured and have the property that if one draws the dual on the same surface, without moving any vertices, the resulting embedding of the complement is also self-dual and all four embeddings are map isomorphic.