MATTHIAS NEUFANG, Carleton University, Ottawa, Ontario K1S 5B6 Operator analogues of various algebras arising in abstract harmonic analysis

In the framework of his concept of an amenable representation, M. B. Bekka has introduced an operator version of the C^* -algebra $\mathrm{LUC}(G)$ of bounded left uniformly continuous functions on a locally compact group G. This C^* -subalgebra of $B(L_2(G))$, denoted by $X(L_2(G))$, contains both $\mathrm{LUC}(G)$ and the compact operators on $L_2(G)$. Using my convolution type product of trace class operators on $L_2(G)$, I present a structural analysis of $X(L_2(G))$. Moreover, the dual $X(L_2(G))^*$ naturally becomes a (completely contractive) Banach algebra. The latter admits a completely isometric representation as completely bounded operators on $B(L_2(G))$; as such, it gives new insight into the representation theoretical programme (carried out by M. Neufang, Z.-J. Ruan and N. Spronk) of studying algebras in abstract harmonic analysis as subalgebras of $CB(B(L_2(G)))$ —such as the measure algebra and the completely bounded multipliers of the Fourier algebra. Finally, the investigations of $X(L_2(G))^*$ lead to what may be considered as a non-commutative analogue of the measure algebra. Extensions of the results to locally compact quantum groups are also discussed.

This is joint work with Z.-J. Ruan.